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Claims

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- 1. A method of fragile watermarking a digital image, including the steps of extracting from the image a portion thereof A and generating at least a first ill-conditioned operator related to values extracted from the portion A.
- A method of fragile watermarking according to claim 1 wherein the ill-conditioned operator is generated by
 altering a value to increase the operator's condition number.
- 3. A method of fragile watermarking according to claim 1 or 2, comprising the step of replacing a non-zero singular value of a singular value matrix S_A of an image or portion thereof A, with a solution to a linear equation comprising the ill-conditioned operator.
- 4. A method of fragile watermarking according to claim 3, 20 wherein the non-zero singular value to be replaced is the smallest non-zero singular value $S_r(A)$ in a singular value matrix S_A of rank r.
- 5. A method of fragile watermarking according to any one of the preceding claims, wherein a non-zero singular value of a singular value matrix S_W of a watermark pattern or portion thereof W is replaced, such that said replacement increases the condition number of the singular value matrix S_W of the watermark pattern or portion thereof W.

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6. A method of fragile watermarking according to claim 5, wherein the non-zero singular value to be replaced is the smallest non-zero singular value $S_t(W)$ in a singular value matrix S_W of rank t.

7. A method of fragile watermarking according to any one of the preceding claims, wherein the step of calculating a replacement non-zero singular value of singular value

5 matrix S_W of a watermark or portion thereof W comprises calculating substantially the following equation part:

$$s_r(W) = \varepsilon$$
,

where ε is a small positive real number that increases the condition number of the singular value matrix S_W .

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8. A method of fragile watermarking according to any one of the preceding claims, wherein the step of generating at least a first ill-conditioned operator comprises calculating substantially the following equation part:

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$$B = \hat{A}\hat{W} ,$$

where \hat{W} is substantially constructed according to $\hat{W} = U_w \hat{S}_w V_w^T$, \hat{S}_w comprising at least one altered singular value $s_t(W) = \varepsilon$, and such that B forms a parametric family of matrices $B(\hat{S}_r) = \hat{A}(\hat{S}_r)\hat{W}$ for possible values of $\hat{S}_r(A)$.

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- 9. A method of fragile watermarking according to claim 8, wherein $s_r(A)$ is determined by an L_2 -norm solution of the least squares problem $\frac{\min}{x \in \Re^p} \|Bx b\|_2^2$ to equal the square of a predefined key N of predetermined value, where b is an arbitrary vector.
- 10. A method of fragile watermarking according to any one of the preceding claims, wherein the step of calculating the replacement non-zero singular value of singular value matrix A comprises calculating substantially the following equation part:

$$\min_{\hat{S}_r(A)} \left\{ \sum_{i=1}^q \left(u_{B_i}^T b / S_I(B(\hat{S}_r)) \right)^2 - N^2 \right\},$$

where u_{B_t} is the I-th column of the matrix formed with the right singular vectors of B.

5 11. A method of fragile watermarking according to claim 10, wherein $\hat{s}_r(A)$ further satisfies $\hat{s}_r(A) = \overline{s}_r(A) \in [\max{(eps, s_r(A) - \delta)}, s_r(A) + \delta] = [H_0, H_1]$, where δ is a distortion control and eps is machine precision, such that the step of calculating the replacement non-zero singular value comprises calculating substantially the following equation part:

$$\sin_{\hat{S}_{r}} \in [H_{0}, H_{1}] \left\{ \sum_{i=1}^{q} \left(u_{B_{i}}^{T} b / S_{i}(B(\hat{S}_{r})) \right)^{2} - N^{2} \right\},$$

with all terms as defined herein.

- 15 12. A method of fragile watermarking according to any one of claims 9 to 11, wherein vector b is related to at least a first parameter derived from a portion of an image I other than A.
- 13. A method of fragile watermarking according to claim 12, wherein for a sequential watermarking process comprising the watermarking of portion $A^{(k)}$ after the watermarking of portion $A^{(k-1)}$, k=1,...,L of L portions, then the step of calculating $b^{(k)}$ for portion $A^{(k)}$ comprises
- 25 calculating substantially the following equation part:

$$b^{(k)} = \begin{cases} A^{(k)}Z^{(k)} & \text{for } k = 1\\ A^{(k-1)}Z^{(k)} & \text{else} \end{cases}$$

where Z^(k) is a pseudo-random binary vector.

14. A method of fragile watermarking according to any one of the preceding claims, wherein the step of calculating the watermarked image or portion thereof \hat{A} comprises calculating substantially the following equation part:

$$\hat{A} = U_{A} \hat{S}_{A} V_{A}^{T}$$

where \hat{S}_A comprises at least one replaced singular value, U_A and V_A being left and right singular matrices.

- 15. A method of fragile watermarking according to any one of the preceding claims, wherein a watermark pattern or portion thereof W is generated by a pseudo-random generator seeded by a key K of predetermined value.
- 16. A method of fragile watermarking according to claim 15. 15, wherein the values of key K and key N are related.
- 17. A method of fragile watermarking according to either one of claims 15 and 16, wherein the a watermark pattern or portion thereof W is generated by a pseudo-random generator seeded by a key K of predetermined value, combined with either a single or repeated instance of a logo.
 - 18. A method of fragile watermarking according to any one of the preceding claims, comprising the following steps;
- 25 i. generating a K-dependent watermark pattern W from Ω , or recalling a pre-existing one;
 - ii. constructing a parametric family of matrices $B(\hat{s}_r)$;
 - iii. estimating a unique parameter $\overline{s}_{r}(A)$, that minimizes the expression

$$\lim_{\hat{S}_r} \left\{ \sum_{i=1}^q \left(u_{B_i}^T b / S_i(B(\hat{S}_r)) \right)^2 - N^2 \right\}; \text{ and}$$

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- iv. estimating the watermarked block $\hat{A} = U_A \hat{S}_A V_A^T$ by setting $\hat{S} = diag(s_1(A), \ldots, s_{r-1}(A), \overline{s}_r(A))$.
- 19. A method of fragile watermarking according to any one of claims 1 to 17, comprising the following steps;
 - i. generating a K-dependent watermark pattern W from Ω , or recalling a pre-existing one;
 - ii. constructing a parametric family of matrices $B(\hat{s}_r)$;
 - iii. estimating a unique parameter $\overline{s}_r(A) \in \left[\max\left(eps,\,s_r(A)\,-\,\delta\right)\,,\,s_r(A)\,+\,\delta\right] = \left[H_0,\,H_1\right], \text{ that minimizes the expression:}$

$$\min_{\hat{S}_{r} \in [H_{0,r}, H_{1}]} \left\{ \sum_{i=1}^{q} \left(u_{B_{i}}^{T} b / S_{i} (B(\hat{S}_{r})) \right)^{2} - N^{2} \right\}; \text{ and}$$

iv. estimating the watermarked block $\hat{A} = U_A \hat{S}_A V_A^T$ by setting $\hat{S} = diag(s_1(A), \ldots, s_{r-1}(A), \overline{s}_r(A))$.

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- 20. A method of verifying a fragile watermark, characterised by the step of generating at least a first ill-conditioned operator by altering a value to increase its condition number, said ill-conditioned operator being related to values extracted from a received image or portion thereof A*.
- 21. A method of verifying a fragile watermark according to claim 20, characterised by the step of calculating a
- 25 solution to the least squares problem $\frac{\min}{x \in \Re^p} \| B x b \|_2^2 \text{ where}$ $B = A \hat{W}.$
 - 22. A method of verifying a fragile watermark according to either one of claims 20 and 21, wherein a positive square-

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root N of the L₂-norm solution of the least squares problem $\frac{\min}{x \in \Re^p} \|B^*x - b\|_2^2 \text{ is compared with key } N; \text{ and }$

the received image or portion thereof A comprising the fragile watermark is declared authentic if $\left|N^*-N\right| \leq \tau$, where τ is a threshold value.

23. A method of verifying a fragile watermark according to any one of claims 20 to 22, wherein the step of calculating value N comprises calculating substantially the following equation part:

$$(N^{\cdot})^{2} = \sum_{i=1}^{n} \left(u_{n_{i}}^{T} b / s_{i}(B^{\cdot}) \right)^{2};$$

N is compared with key N; and

the received image or portion thereof A comprising the fragile watermark is declared authentic if $\left|N^*-N\right| \leq \tau$,

15 where τ is a threshold value.

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- 24. Apparatus for fragile watermarking of an image in accordance with a method of any one of claims 1 to 19, comprising generating means for generating at least a first ill-conditioned operator, said ill-conditioned operator being related to values extracted from an image or portion thereof A.
- 25. Apparatus for validating a fragile watermarked image 25 in accordance with a method of any one of claims 20 to 23, and comprising;

generating means for generating at least a first illconditioned operator by altering a value to increase its condition number, said ill-conditioned operator being WO 2005/015493 PCT/EP2004/051265

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related to values extracted from a received image or portion thereof \mathbf{A}^{\bullet} .